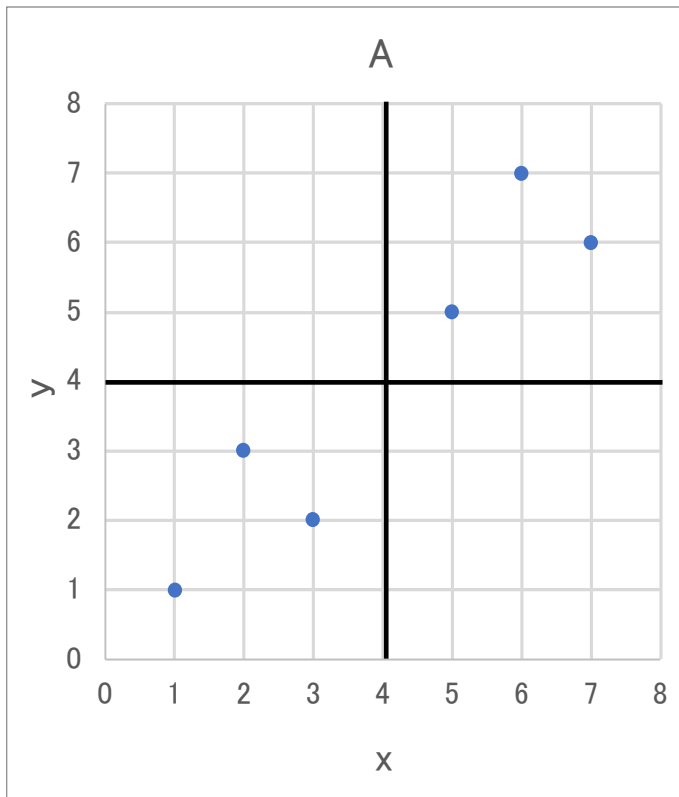


	x	A	B
	7	6	1
	6	7	6
	5	5	5
	3	2	7
	2	3	2
	1	1	3
	0		
平均値	4	4	4
標準偏差	2.16	2.16	2.16

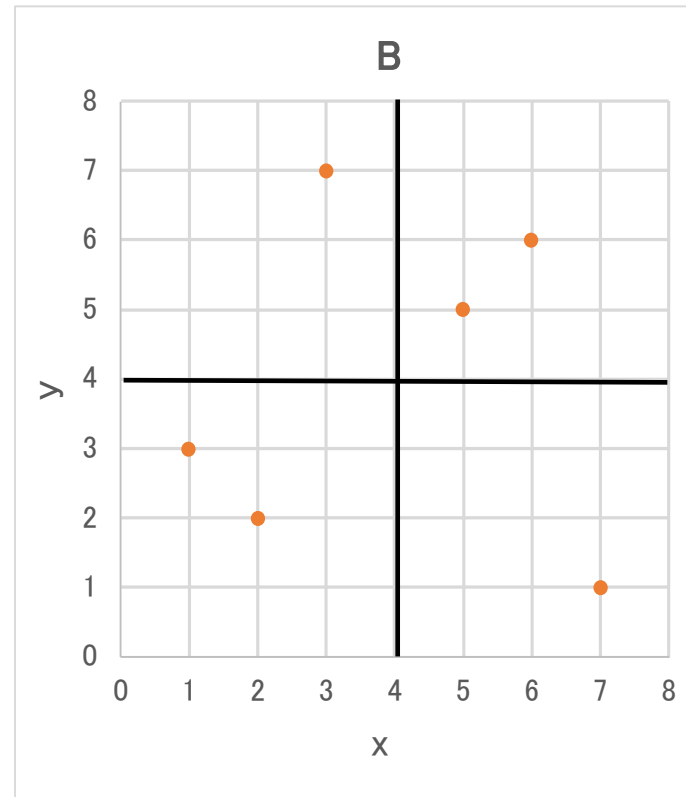
$x_i - \bar{x}$	$y_{Ai} - \bar{y}_A$	$y_{Bi} - \bar{y}_B$
3	2	-3
2	3	2
1	1	1
-1	-2	3
-2	-1	-2
-3	-3	-1

	$(x_i - \bar{x})(y_{Ai} - \bar{y}_A)$	$(x_i - \bar{x})(y_{Bi} - \bar{y}_B)$
	6	-9
	6	4
	1	1
	2	-3
	2	4
	9	3
合計/6	4.33	0

相関係数	0.93	0.00
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共分散 : 4.33  
相関係数 : 0.93



共分散 : 0  
相関係数 : 0.00

相関係数 =  $\frac{\text{共分散}}{(x\text{の標準偏差}) \times (y\text{の標準偏差})}$   
 $\frac{4.33}{2.16 \times 2.16}$

$$\frac{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2} \times \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \bar{y})^2}} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \times \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}$$

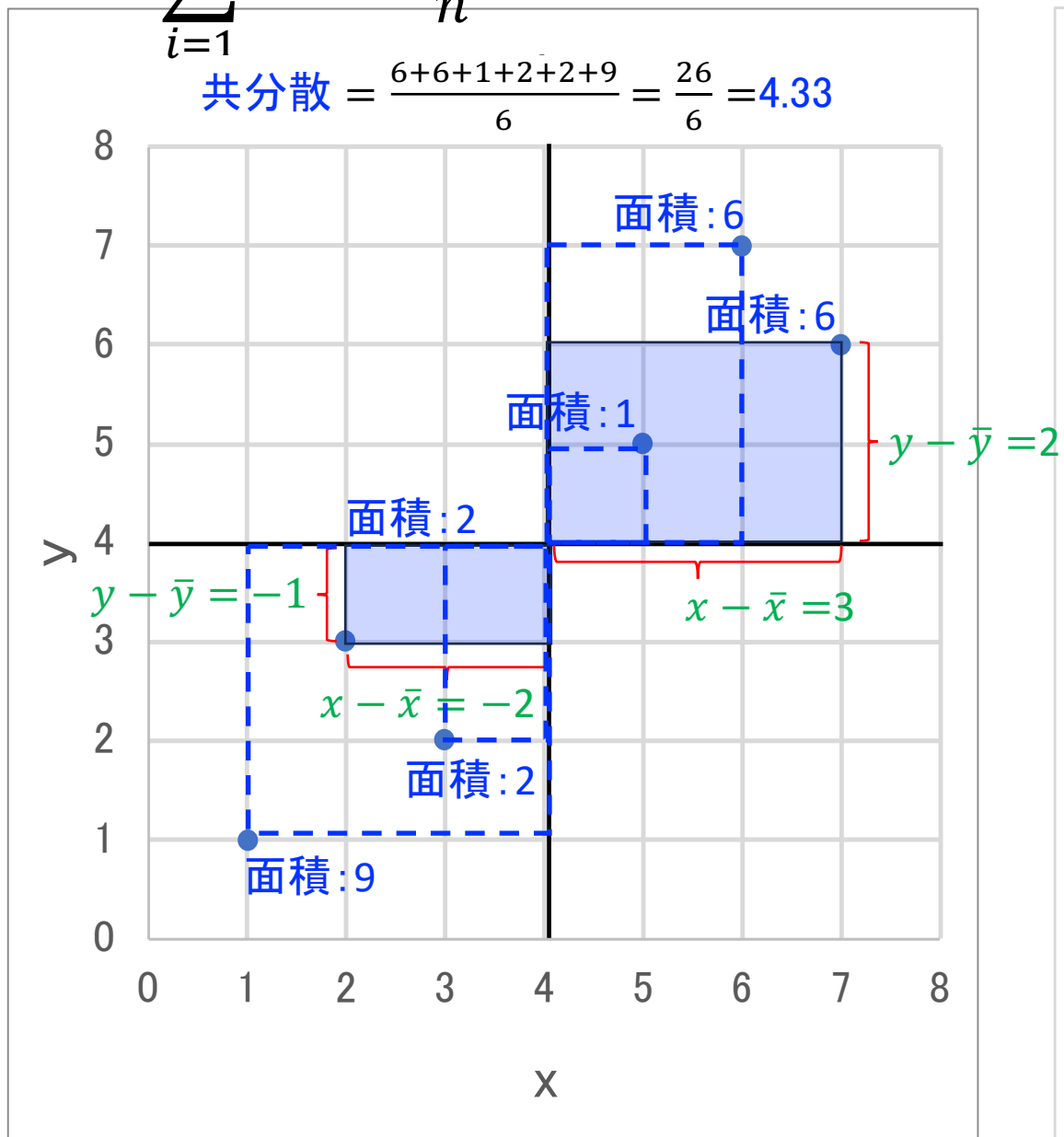
分母が同じでも共分散で相関関係がわかる

← 共分散

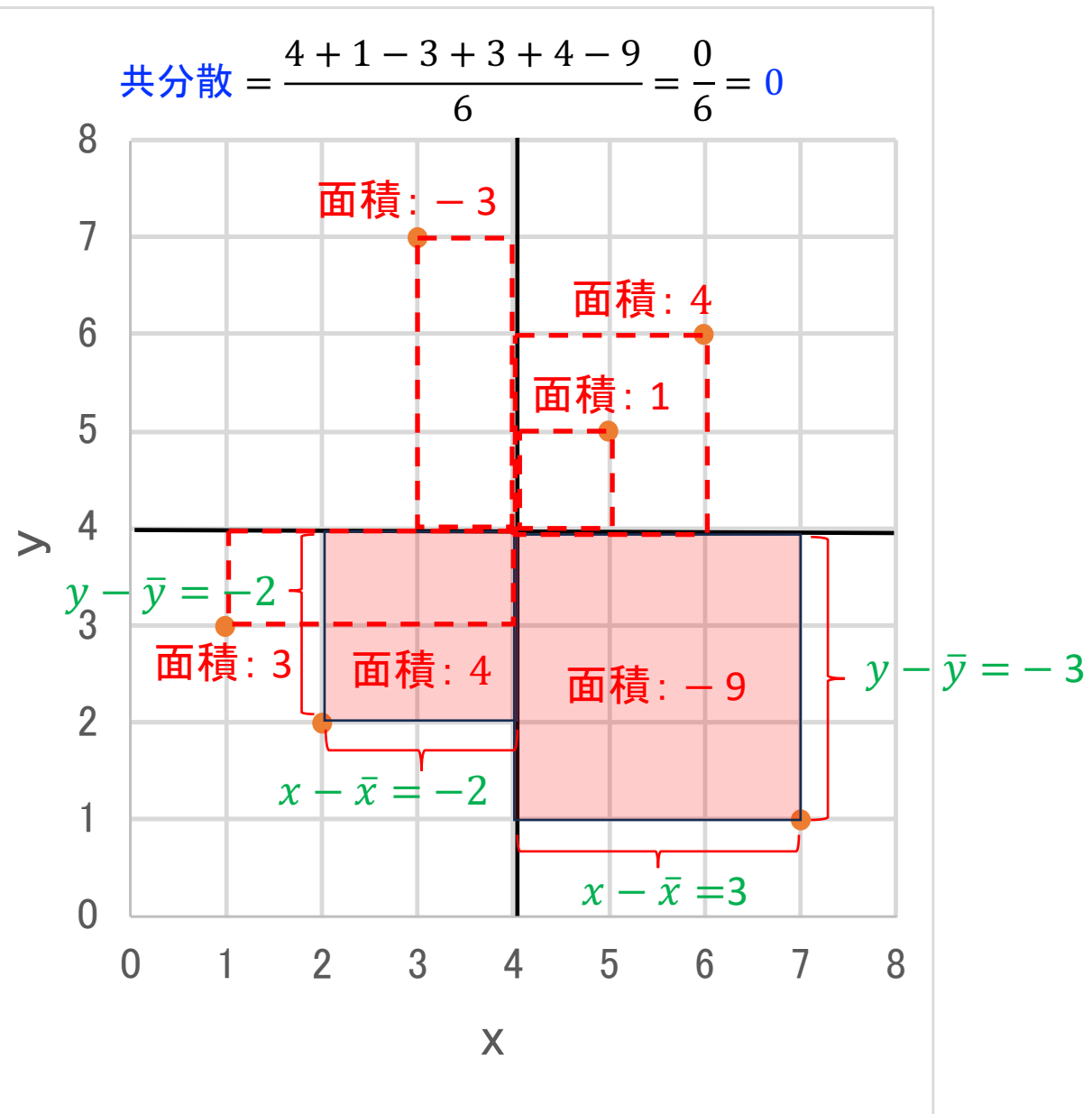
$$\text{共分散} = \sum_{i=1}^n \frac{(x_i - \bar{x})(y_i - \bar{y})}{n}$$

$$\text{面積} = (x_i - \bar{x})(y_i - \bar{y})$$

$$\text{共分散} = \frac{6+6+1+2+2+9}{6} = \frac{26}{6} = 4.33$$



$$\text{共分散} = \frac{4 + 1 - 3 + 3 + 4 - 9}{6} = \frac{0}{6} = 0$$



相関係数 =  $\frac{\text{共分散}}{(x\text{の標準偏差}) \times (y\text{の標準偏差})} = \frac{1}{n} \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sigma_x \cdot \sigma_y} = \frac{1}{n} \frac{\sum_{i=1}^n (x_i - \bar{x})}{\sigma_x} \cdot \frac{\sum_{i=1}^n (y_i - \bar{y})}{\sigma_y}$  ← 四角形の辺の長さを標準化 → 面積も標準化

	x	A	B
	7	12	3
	6	14	18
	5	10	15
	3	4	21
	2	6	6
	1	2	9
	0		
平均値	4	8	12
標準偏差	2.16	4.32	6.48

$x_i - \bar{x}$	$y_{Ai} - \bar{y}_A$	$y_{Bi} - \bar{y}_B$
3	4	-9
2	6	6
1	2	3
-1	-4	9
-2	-2	-6
-3	-6	-3

$\frac{(x_i - \bar{x})}{\sigma_x}$	$\frac{(y_{Ai} - \bar{y}_A)}{\sigma_{y_A}}$	$\frac{(y_{Bi} - \bar{y}_B)}{\sigma_{y_B}}$
1.39	0.93	-1.39
0.93	1.39	0.93
0.46	0.46	0.46
-0.46	-0.93	1.39
-0.93	-0.46	-0.93
-1.39	-1.39	-0.46

